

## Additional Material for Circular Motion

**Uniform circular motion:** It is a motion of an object on a circular path with a constant speed.

Below are a few examples of circular motion.

**Ex:** 1) Motion of the earth around the sun.

2) Motion of the satellites around the planets.

3) Motion of the blades of a fan.

In uniform circular motion, magnitude of velocity is constant but its direction changes continuously. Since there is a change in the direction of velocity we can say that the object is being accelerated.

Below are the formulae to calculate:

**Linear velocity:**  $v = 2\pi r / t$

**Angular Velocity :**  $\omega = v/r$

**Centripetal Acceleration:**  $a_c = \omega^2 r$

**Centripetal Force:**  $F_c = mv^2/r$

**Q1.** Consider the white point as a toy car of mass 1 Kg that moves on a circular track of radius 8.00 m in 10.0 seconds. Calculate the centripetal acceleration of the car.

**Solution:** given data: mass = 1 kg

radius = 8 m

time period = 10 s

Formula to calculate linear velocity:

$$v = \frac{2\pi r}{t}$$
$$= \frac{2 \times 3.14 \times 8}{10}$$

$$= 5.024 \text{ m/s}$$

Formula to calculate Angular velocity:

$$\begin{aligned}\omega &= v/r \\ &= 5.024/8 \\ &= 0.628 \text{ rad/s}\end{aligned}$$

Using the values of angular velocity and radius we can calculate centripetal acceleration.

$$\begin{aligned}a_c &= \omega^2 r \\ &= (0.628)^2 \times 8 \\ &= 3.15 \text{ m/s}^2\end{aligned}$$

### **Answers to the Assignment Numericals**

1)  $v = 1.25 \text{ m/s}$

$$\omega = 0.628 \text{ rad/s}$$

2)  $v = 7.85 \text{ m/s}$

$$\omega = 0.78 \text{ rad/s}$$

$$F_c = 12.32 \text{ N}$$

3)  $F_c = 4.85 \text{ N}$  (Hint: change the values according to numerical in the App. Use the values of velocity and radius from the App to calculate centripetal force.)